

Objectives: Our goal is to learn how to graph a quadratic equation in any form.

Three different forms of a quadratic function:

Vertex Form: $\text{Vertex } (h, k)$
 $f(x) = a(x - h)^2 + k$

Intercept Form: $(p, 0) (q, 0)$
 $f(x) = a(x - p)(x - q)$

Standard Form:
 $f(x) = ax^2 + bx + c$

complete the square factor

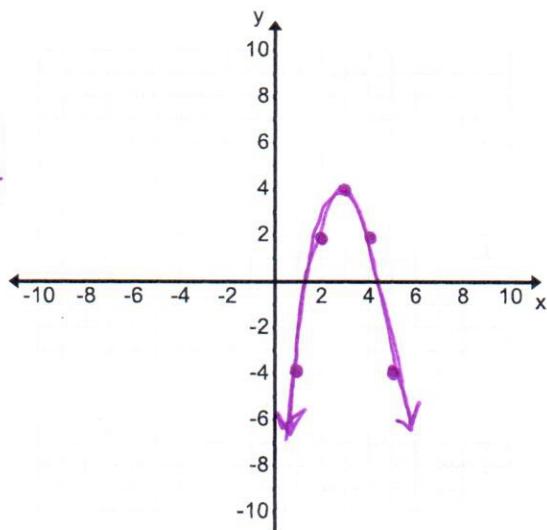
Example 1: Graph the following quadratic function given in vertex form.

$$a(x-h)^2+k$$

$$y = -2(x-3)^2 + 4$$

x	y
1	-4
2	2
3	4
4	2
5	-4

$$\begin{aligned} -2(1-3)^2+4 \\ -2(2-3)^2+4 \end{aligned}$$



vertex: $(3, 4)$

x-int when $y=0$

$$0 = -2(x-3)^2 + 4$$

$$-4 = -2(x-3)^2$$

$$\frac{-4}{-2} = \frac{-2(x-3)^2}{-2}$$

$$\sqrt{2} = \sqrt{(x-3)^2}$$

$$x-3 = \pm\sqrt{2}$$

$$x = 3 + \sqrt{2} \quad x = 3 - \sqrt{2}$$

y-int when $x=0$

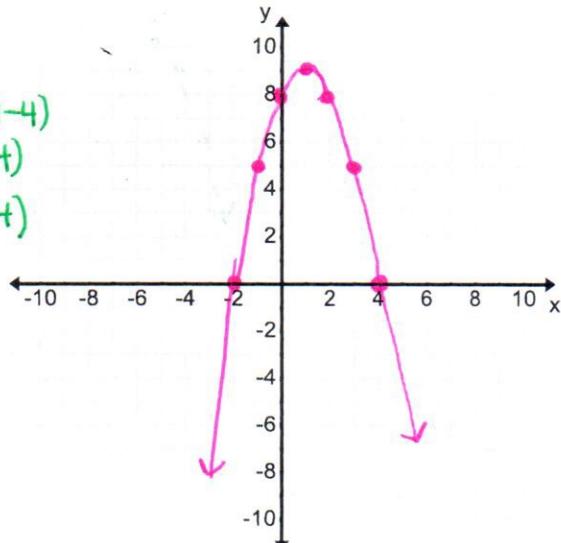
$$\begin{aligned} y &= -2(0-3)^2 + 4 \\ &= -14 \end{aligned}$$

Example 2: Graph the following quadratic function given in intercept form.

$$y = -(x+2)(x-4)$$

x	y
-1	5
0	8
1	9
2	8
3	5

$$\begin{aligned} -(-1+2)(-1-4) \\ -(0+2)(0-4) \\ -(1+2)(1-4) \end{aligned}$$



vertex

$$h = \frac{-2+4}{2} = 1$$

Identify Critical Information:

Vertex (Max/Min):

Max @ $(3, 4)$

Axis of Symmetry:

$$x=3$$

Y-Int:

$$(0, -14)$$

X-Int:

$$(3+\sqrt{2}, 0)$$

$$(3-\sqrt{2}, 0)$$

Domain:

$$(-\infty, \infty)$$

Range:

$$(-\infty, 4]$$

Identify Critical Information:

Vertex (Max/Min):

Max @ $(1, 9)$

Axis of Symmetry:

$$x=1$$

Y-Int:

$$(0, 8)$$

X-Int:

$$(-2, 0)(4, 0)$$

Domain:

$$(-\infty, \infty)$$

Range:

$$(-\infty, 9]$$

Example 3: Graph the following quadratic function given in standard form.

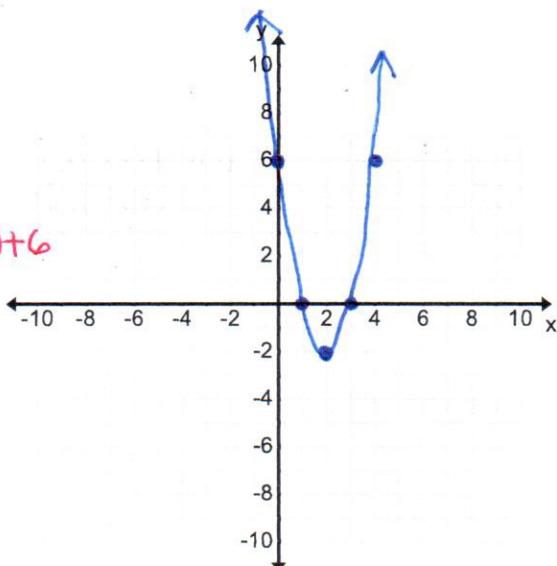
$$y = 2x^2 - 8x + 6$$

x	y
0	6
1	0
2	-2
3	0
4	6

Vertex: (h, k)

$$h = \frac{-b}{2a} = \frac{+8}{2(2)} = 2$$

$$2(2)^2 - 8(2) + 6$$



Identify Critical Information:

Vertex (Max/Min):

MIN @ $(2, -2)$

Axis of Symmetry:

$$x = 2$$

Y-Int: $(0, 6)$

X-Int:

$$(1, 0) \quad (3, 0)$$

Domain:

$$(-\infty, \infty)$$

Range:

$$[-2, \infty)$$

Identify Critical Information:

Vertex (Max/Min):

MAX @ $(1, -2)$

Axis of Symmetry:

$$x = 1$$

Y-Int: $(0, -3)$

X-Int:

NONE

Domain:

$$(-\infty, \infty)$$

Range:

$$(-\infty, -2]$$

Example 4: Graph the following quadratic function given in standard form.

$$y = -x^2 + 2x - 3$$

x	y
-1	-6
0	-3
1	-2
2	-3
3	-6

