

Chapter 13 Review

Factor each completely.

1) $4a^3 - 48a^2 + 128a$

$$4a(a^2 - 12a + 32)$$

$$4a(a-4)(a-8)$$

Simplify each expression.

3) $\frac{n^2 - 6n - 7}{n^2 - 4n - 21}$

$$\frac{(n-7)(n+1)}{(n-7)(n+3)}$$

$$\frac{(n-7)(n+1)}{(n-7)(n+3)}$$

$$= \frac{n+1}{n+3}$$

2) $5m^2 + 2m - 7$

$$\begin{array}{l} \boxed{ac} \\ -35 \\ \hline 5, -7 \\ -5, 7 \end{array} \quad \begin{array}{l} 5m^2 - 5m + 7m - 7 \\ 5m(m-1) + 7(m-1) \\ \boxed{(5m+7)(m-1)} \end{array}$$

4) $\frac{3r^3 + 3r^2 - 6r}{6r^3 + 18r^2 + 12r}$

$$\frac{3r(r^2+r-2)}{6r(r^2+3r+2)} = \frac{\cancel{3}r(r-1)(r+2)}{2\cancel{3}r(r+1)(r+2)}$$

$$= \frac{r-1}{2(r+1)}$$

5) $\frac{n^2 - 13n + 36}{6} \cdot \frac{5}{5n - 20}$

$$\frac{(n-9)(n-4)}{6} \rightarrow \frac{5}{5(n-4)}$$

$$\frac{\cancel{1}5(n-9)(\cancel{n-4})}{6\cancel{3}0(n-4)}$$

$$\frac{n-9}{6}$$

6) $\frac{7n+5}{n^2 - 11n + 28} \cdot \frac{2n-14}{14n+10}$

$$\frac{(7n+5)}{(n-7)(n-4)} \rightarrow \frac{2(n-7)}{2(7n+5)}$$

$$\frac{\cancel{2}(7n+5)(\cancel{n-7})}{2(n-7)(n-4)(\cancel{7n+5})} = \frac{1}{n-4}$$

$$7) \frac{6x^2 + 21x}{14x^3 + 49x^2} \div \frac{1}{7x^2}$$

$$\frac{3x(2x+7)}{7x^2(2x+7)} \div \frac{1}{7x^2}$$

$$\frac{3x(2x+7)}{7x^2(2x+7)} \rightarrow \frac{7x^2}{7x^2(2x+7)} \rightarrow 1$$

$$\frac{3\cancel{x}(2x+7)}{7x^2(2x+7)} = \frac{3x}{1} = \boxed{3x}$$

$$8) \frac{12x - 30}{4x^2 - 8x - 5} \div \frac{6x - 12}{4x + 2}$$

$$\frac{2(x-15)}{4x^2 - 8x - 5} \div \frac{6(x-2)}{2(2x+1)}$$

ac
-20
4, -5
-10, 2

$$(2x+1)(2x-5)$$

$$\frac{6(2x-5)}{(2x+1)(2x-5)} \rightarrow \frac{2(2x+1)}{6(x-2)} = \frac{2(2x+1)}{6(2x+1)(2x-5)(x-2)}$$

$$= \boxed{\frac{2}{x-2}}$$

$$\frac{2y^2}{2y^2} \cdot \frac{4x}{4y} + \frac{5x}{2y^2} \cdot \frac{4y}{4y}$$

$$\frac{8xy^2}{8y^3} + \frac{20xy}{8y^3}$$

$$\boxed{\frac{8xy^2 + 20xy}{8y^3}}$$

$$\text{OR } \frac{4xy^2 + 10xy}{4y^3}$$

$$\frac{(b+5)}{(b+5)} \cdot \frac{6}{2b-1} + \frac{3}{b+5} \cdot \frac{(2b-1)}{(2b-1)}$$

$$\frac{6(b+5)}{(b+5)(2b-1)} + \frac{3(2b-1)}{(b+5)(2b-1)}$$

$$\frac{6b+30+6b-3}{(b+5)(2b-1)} = \boxed{\frac{12b+27}{(b+5)(2b-1)}}$$

$$\frac{5}{5} \cdot \frac{x+5y}{2x} - \frac{4x}{5} \cdot \frac{2x}{2x}$$

$$\frac{5(x+5y)}{10x} - \frac{8x^2}{10x}$$

$$\boxed{\frac{5x+25y-8x^2}{10x}}$$

$$\frac{(p+6)}{(p+6)} \cdot \frac{2p}{p-5} - \frac{5}{p+6} \cdot \frac{(p-5)}{(p-5)}$$

$$\frac{2p(p+6)}{(p+6)(p-5)} - \frac{5(p-5)}{(p+6)(p-5)}$$

$$\frac{2p^2 + 12p - (5p - 25)}{(p+6)(p-5)} = \boxed{\frac{2p^2 + 7p + 25}{(p+6)(p-5)}}$$