

1-2 Find the measure of angle A

1. Angle Sum Theorem

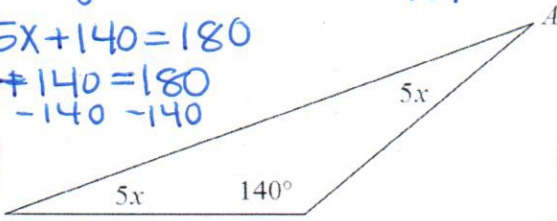
$$\begin{aligned} 5x + 5x + 140 &= 180 \\ 10x + 140 &= 180 \\ -140 \quad -140 & \end{aligned}$$

$$\frac{10x}{10} = \frac{40}{10}$$

$$x = 4$$

$$m\angle A = 5(4)$$

$$m\angle A = 20^\circ$$



2. Angle Sum Theorem

$$2x + 8 + 6x - 6 + 90 = 180$$

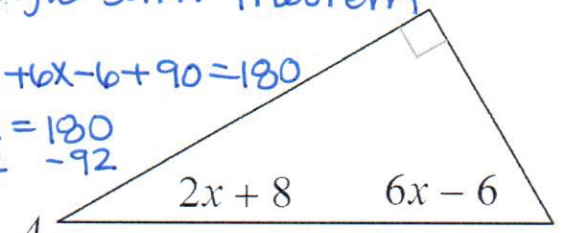
$$\begin{aligned} 8x + 92 &= 180 \\ -92 \quad -92 & \end{aligned}$$

$$\frac{8x}{8} = \frac{88}{8}$$

$$x = 11$$

$$m\angle A = 2(11) + 8$$

$$m\angle A = 30^\circ$$



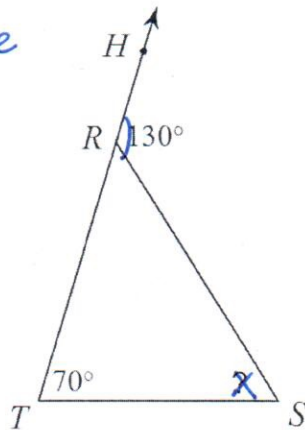
3. Find  $m\angle S$

Exterior Angle Theorem

$$\begin{aligned} 130 &= 70 + x \\ -70 \quad -70 & \end{aligned}$$

$$x = 60^\circ$$

$$m\angle S = 60^\circ$$



4. Find  $m\angle B$

Exterior Angle Thm

$$8x + 18 = 40 + 5x + 14$$

$$\begin{aligned} 8x + 18 &= 5x + 54 \\ -18 \quad -18 & \end{aligned}$$

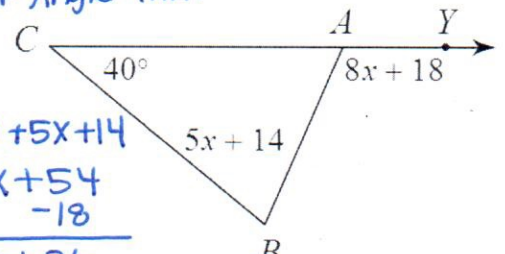
$$8x = 5x + 36$$

$$\begin{aligned} -5x \quad -5x & \\ \hline 3x &= 36 \\ \frac{3x}{3} &= \frac{36}{3} \end{aligned}$$

$$x = 12$$

$$m\angle B = 5(12) + 14$$

$$m\angle B = 74^\circ$$



5. Find  $m\angle W$

Exterior Angle Thm

$$9x = 2x + 20 + 64$$

$$9x = 2x + 84$$

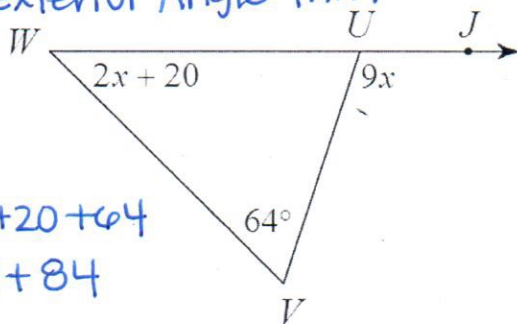
$$\begin{aligned} -2x \quad -2x & \\ \hline 7x &= 84 \end{aligned}$$

$$\frac{7x}{7} = \frac{84}{7}$$

$$x = 12$$

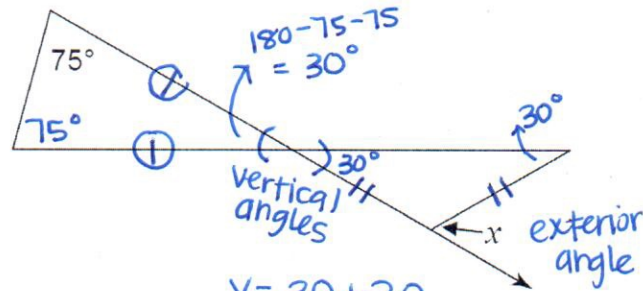
$$m\angle W = 2(12) + 20$$

$$m\angle W = 44^\circ$$



6. Find measure of  $\angle x$

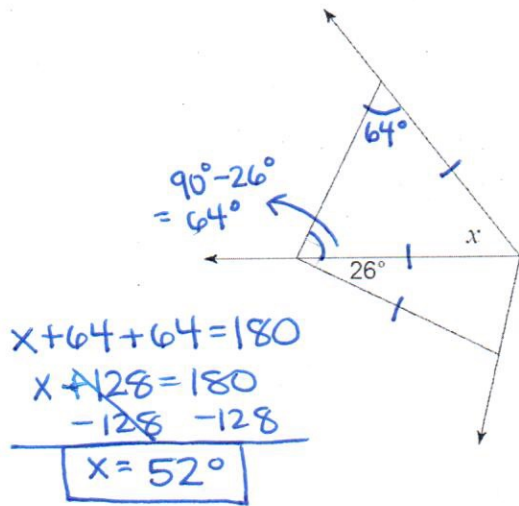
Isosceles  $\Delta$  Thm



$$x = 30 + 30$$

$$x = 60^\circ$$

7. Find measure of  $\angle x$ .

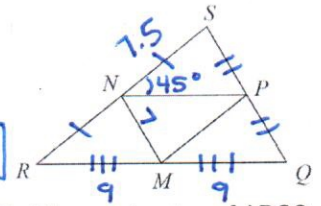


### Midsegment Thm

8. Given that points N, P, & M are mid points, and given  $\overline{NM} = 7, \overline{RQ} = 18, \angle SNP = 45^\circ$

a. Find the length of NP

$$\begin{aligned} 2\overline{NP} &= \overline{RQ} \\ \frac{2\overline{NP}}{2} &= \frac{18}{2} \\ \overline{NP} &= 9 \end{aligned}$$



b. Given that  $\overline{SN} = 7.5$ , Find the perimeter of  $\triangle RSQ$

$$\begin{aligned} \overline{SN} = \overline{RN} &= 7.5 \text{ so } \overline{RS} = 15 \\ \overline{RM} = \overline{MQ} &= 9 \text{ so } \overline{RQ} = 18 \\ \overline{NM} &= 7 \quad \overline{SQ} = 2(7) = 14 \\ \text{perimeter } \triangle RSQ &= 15 + 18 + 14 = 47 \end{aligned}$$

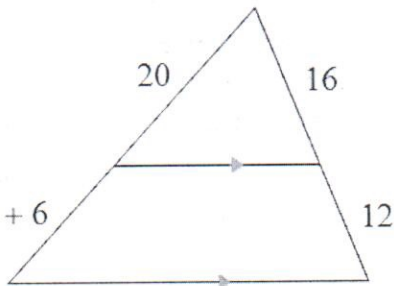
c. Find  $\angle SRQ$

$\overline{NP} \parallel \overline{RQ}$  and  $\overline{RS}$  is a transversal so by corresponding angles  $m\angle SRQ = 45^\circ$

9. Solve for x.

### Triangle Proportionality Thm

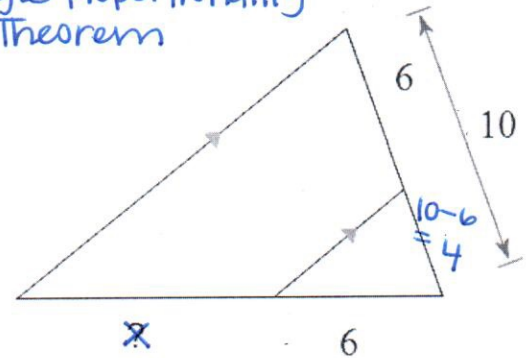
$$\frac{20}{x+6} = \frac{16}{12}$$



$$\begin{aligned} 240 &= 16(x+6) \\ 240 &= 16x + 96 \\ -96 \quad -96 \\ \hline 144 &= 16x \\ \frac{144}{16} &= \frac{16x}{16} \\ x &= 9 \end{aligned}$$

10. Find the missing side length.

### Triangle Proportionality Theorem

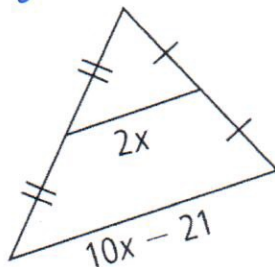


$$\frac{4}{6} = \frac{6}{x}$$

$$\frac{4x}{4} = \frac{36}{4} \quad x = 9$$

11. Solve for x.

### Midsegment Theorem



$$2(2x) = 10x - 21$$

$$4x = 10x - 21$$

$$\begin{aligned} -10x & \quad -10x \\ \hline -6x & = -21 \\ \frac{-6x}{-6} & = \frac{-21}{-6} \end{aligned}$$

$$x = 3.5$$

12. Solve for x.

### Angle Bisector Theorem

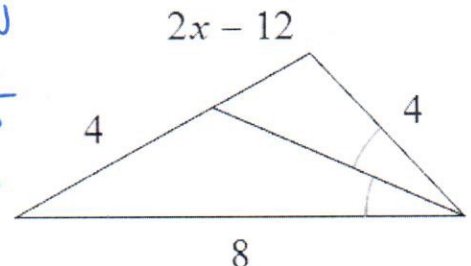
$\frac{\text{opp}}{\text{adj}}$

$$\frac{2x-12}{4} = \frac{4}{8}$$

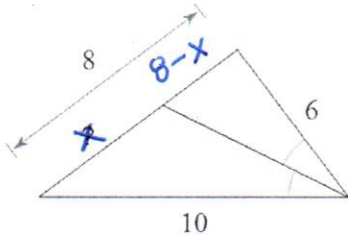
$$8(2x-12) = 16$$

$$16x - 96 = 16$$

$$\begin{aligned} +96 \quad +96 \\ \hline 16x & = 112 \\ \frac{16x}{16} & = \frac{112}{16} \\ x & = 7 \end{aligned}$$



13. Find the missing side length.  
Angle Bisector Thm



$$\frac{8-x}{6} = \frac{x}{10}$$

$$6x = 10(8-x)$$

$$6x = 80 - 10x$$

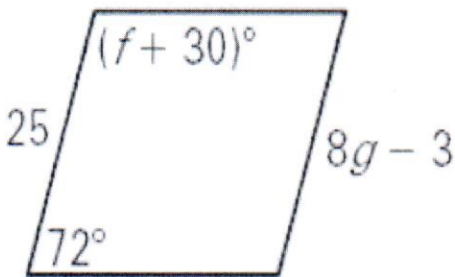
$$+10x \quad +10x$$

$$16x = 80$$

$$\frac{16x}{16} = \frac{80}{16}$$

$$x = 5$$

15. Given the parallelogram, solve for f and g.  
opposite sides are  $\cong$   
same side interior angles



$$\frac{25}{+3} = \frac{8g-3}{+3}$$

$$\frac{28}{8} = \frac{8g}{8}$$

$$g = 3.5$$

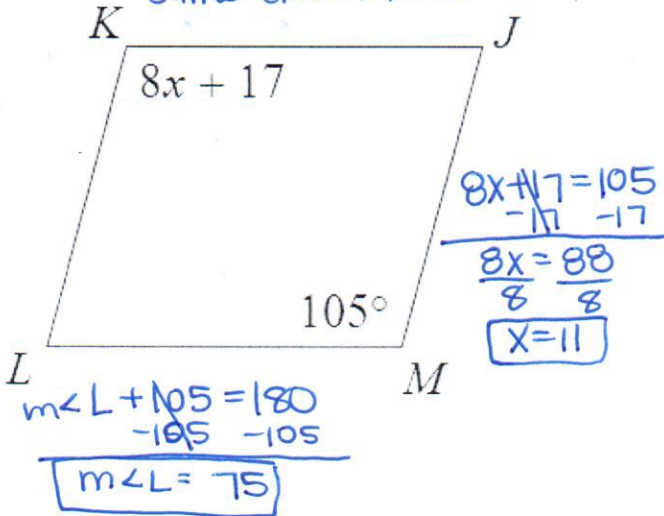
$$72 + f + 30 = 180$$

$$102 + f = 180$$

$$-102 \quad -102$$

$$f = 78$$

17. Given the parallelogram,  
Solve for x and find  $m\angle L$ .  
opposite angles are  $\cong$   
same side interior



$$8x+17 = 105$$

$$-17 \quad -17$$

$$\frac{8x}{8} = \frac{88}{8}$$

$$x = 11$$

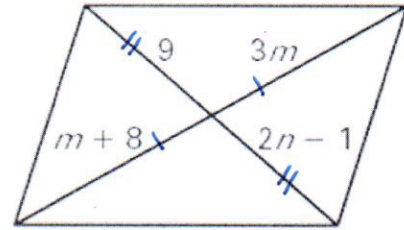
$$m\angle L + 105 = 180$$

$$-105 \quad -105$$

$$m\angle L = 75$$

14. Given the parallelogram,  
solve for m and n.

diagonals  
bisect each  
other



$$9 = 2n-1$$

$$+1 \quad +1$$

$$\frac{10}{2} = \frac{2n}{2}$$

$$n = 5$$

$$3m = m+8$$

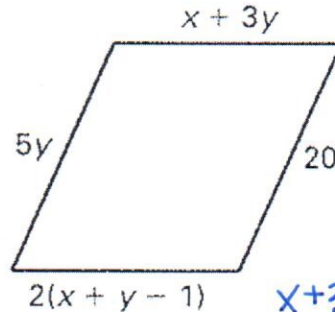
$$-m \quad -m$$

$$\frac{2m}{2} = \frac{8}{2}$$

$$m = 4$$

16. Given the parallelogram,  
solve for x and y.

opposite sides  
are  $\cong$



$$\frac{5y}{5} = \frac{20}{5}$$

$$y = 4$$

$$x+3y = 2(x+y-1)$$

$$x+3y = 2x+2y-2$$

$$y = 4$$

$$x+3(4) = 2x+2(4)-2$$

$$x+12 = 2x+6$$

$$-x+6 = -x+6$$

$$\frac{2x}{x} = \frac{6}{x}$$

$$x = 6$$

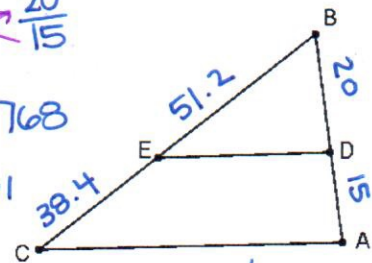
18. BE = 51.2, EC = 38.4, DA = 15,  
BD = 20. Is  $\overline{AC} \parallel \overline{DE}$ ? Justify.

Triangle Proportionality Thm

$$\frac{51.2}{38.4} \stackrel{?}{=} \frac{20}{15}$$

$$768 \stackrel{?}{=} 768$$

yes  
equal



yes,  $\overline{AC} \parallel \overline{DE}$ !

19. Given the vertices  $A(-4,4)$ ,  $B(-2,7)$ ,  $C(2,0)$  Classify the triangle as scalene, isosceles, or equilateral. Is the triangle a right triangle? Explain.

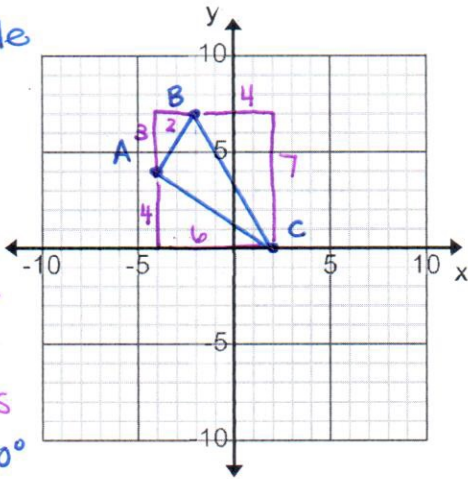
• NONE of the outside  $\Delta$ 's are the same

$m_{AB} = \frac{3}{2}$

$m_{AC} = \frac{-4}{6} = -\frac{2}{3}$

opposite reciprocals

• so  $\angle A = 90^\circ$



SCALENE RIGHT  $\Delta$

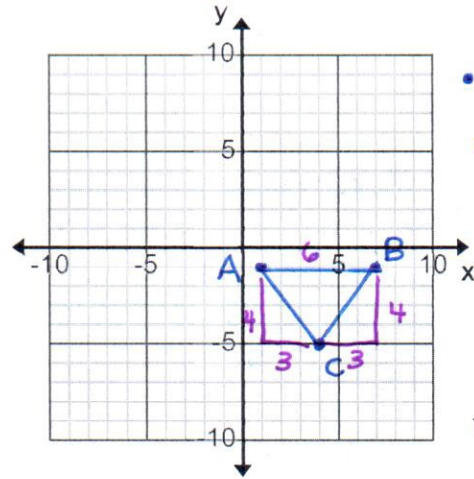
20. Given the vertices  $A(1,-1)$ ,  $B(7,-1)$ ,  $C(4,-5)$  Classify the triangle as scalene, isosceles, or equilateral. Is the triangle a right triangle? Explain.

• Two outside  $\Delta$ 's are  $\cong$ .

$m_{AC} = -\frac{4}{3}$

$m_{CB} = \frac{+4}{+3}$

Not same, not opposite reciprocals



ISOSCELES  $\Delta$

21. What is the most precise classification of the quadrilateral formed by the given vertices:  $T(-3,3)$ ,  $U(1,6)$ ,  $V(1,1)$ , and  $W(-3,-2)$  Show your work.

RHOMBUS

$3^2 + 4^2 = c^2$

$9 + 16 = c^2$

$25 = c^2$

$c = 5$

$\overline{TU} \cong \overline{UV} \cong \overline{VW} \cong \overline{WT}$

all sides are  $\cong$

$m_{TU} = \frac{3}{4}$

$m_{VW} = \frac{3}{4}$

$\overline{TU} \parallel \overline{VW}$

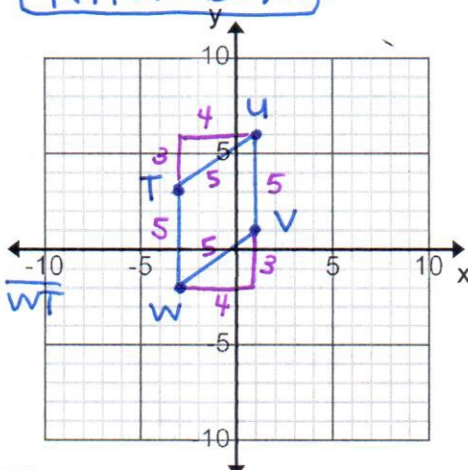
same

$m_{TW} = \frac{5}{0}$

$m_{UV} = \frac{5}{0}$

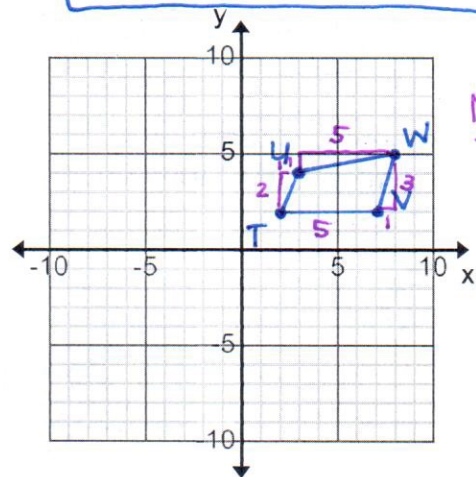
same

opposite sides are parallel



22. Prove or disprove that the given vertices form a parallelogram:  $T(2,2)$ ,  $U(3,4)$ ,  $V(7,2)$ , and  $W(8,5)$ . Show your work.

NOT A PARALLELOGRAM



None of the sides are the same!