

Secondary 3H: 5-2 Notes: Adding and Subtracting Radicals

Warm-Up:

- The volume V of a wooden beam is $V = ls^2$, where l is the length of the beam and s is the length of one side of its square cross section. If the volume of the beam is 1200 in^3 and its length is 96 in . what is the side length? Leave your answer in radical form. Make sure to rationalize the denominator.

$$V = ls^2$$

$$s^2 = \frac{V}{l}$$

$$s = \sqrt{\frac{V}{l}}$$

$$s = \sqrt{\frac{1200}{96}}$$

$$s = \sqrt{\frac{25}{2}} = \frac{\sqrt{25}}{\sqrt{2}} = \frac{\sqrt{50}}{2} = \frac{5\sqrt{2}}{2} \text{ in}$$

Adding and Subtracting Radical Expressions:

- Like radicals with numbers:

$$\sqrt{2} + 3\sqrt{2} = 4\sqrt{2}$$

$$2\sqrt[3]{7} - 5\sqrt[3]{7} = -3\sqrt[3]{7}$$

$$4\sqrt{3} + \sqrt{13} = \text{can't add}$$

radicand is different

- Like radicals with variables:

$$\sqrt{5xy} + 8\sqrt{5xy} = 9\sqrt{5xy}$$

$$\sqrt[3]{9x^2y} - 8\sqrt[3]{9x^2y} = -7\sqrt[3]{9x^2y}$$

How do you know if you have "like" radicals?

- same index
- same radicand

What is really happening when we add or subtract??

- Using the distributive property:

$$a^n\sqrt[n]{x} + b^n\sqrt[n]{x} =$$

$$\sqrt[n]{x} (a+b) = (a+b)\sqrt[n]{x}$$

$$a^n\sqrt[n]{x} - b^n\sqrt[n]{x} =$$

$$\sqrt[n]{x} (a-b) = (a-b)\sqrt[n]{x}$$

Got it?

- What is the simplified form of each expression?

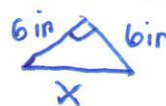
$$3\sqrt{5x} - 2\sqrt{5x} = \sqrt{5x}$$

$$6x^2\sqrt{7} + 4x\sqrt{5} \text{ already simplified}$$

$$12\sqrt[3]{7xy} - 8\sqrt[3]{7xy} = 4\sqrt[3]{7xy}$$

Do you really have it?

- In this stained glass window design, the side of each small square is 6 in . Find the perimeter of the window to the nearest tenth of an inch.

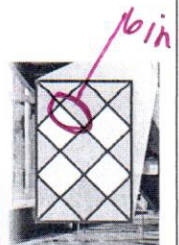


$$6^2 + 6^2 = x^2$$

$$72 = x^2$$

$$x = \sqrt{72}$$

$$P = 10(\sqrt{72}) = 84.9 \text{ in}$$



Simplifying BEFORE adding or subtracting...

- Although you cannot combine radicals with different radicands, it may be possible to simplify the radicals so that the radicands are the same:

$$\begin{aligned} & \bullet \sqrt{12} + \sqrt{75} - \sqrt{3} \\ & \begin{array}{c} \text{4} \quad \text{3} \\ \wedge \quad \wedge \\ \boxed{2} \quad \boxed{2} \end{array} \quad \begin{array}{c} \text{25} \quad \text{3} \\ \wedge \quad \wedge \\ \boxed{5} \quad \boxed{5} \end{array} \\ & 2\sqrt{3} + 5\sqrt{3} - \sqrt{3} \\ & = \boxed{6\sqrt{3}} \end{aligned}$$

Got it?

- Simplify:
 - $\sqrt[3]{250} + \sqrt[3]{54} - \sqrt[3]{16}$

$$\begin{array}{c} \text{3} \quad \text{3} \quad \text{3} \quad \text{2} \quad \text{2} \quad \text{2} \quad \text{2} \\ \wedge \quad \wedge \quad \wedge \quad \wedge \quad \wedge \quad \wedge \\ \boxed{5} \quad \boxed{5} \quad \boxed{5} \quad \boxed{2} \quad \boxed{2} \quad \boxed{2} \end{array}$$

$$5\sqrt[3]{2} + 3\sqrt[3]{2} - 2\sqrt[3]{2} = \boxed{6\sqrt[3]{2}}$$
 - $3\sqrt[3]{81} - 2\sqrt[3]{54}$

$$\begin{array}{c} \text{9} \quad \text{9} \\ \wedge \quad \wedge \\ \boxed{3} \quad \boxed{3} \quad \boxed{3} \quad \boxed{3} \end{array}$$

$$3(3)\sqrt[3]{3} - 2(3)\sqrt[3]{2} = \boxed{9\sqrt[3]{3} - 6\sqrt[3]{2}}$$

Multiplying Binomial Radical Expressions

- How do you think you could multiply the following binomial radical expressions?

double distribution "FOIL"

$$(4 + 2\sqrt{2})(5 + 4\sqrt{2})$$

$$20 + 16\sqrt{2} + 10\sqrt{2} + 8(\sqrt{2})^2$$

$$\boxed{36 + 26\sqrt{2}}$$

$$(3 - \sqrt{7})(5 + \sqrt{7})$$

$$15 + 3\sqrt{7} - 5\sqrt{7} - 7$$

$$\boxed{8 - 2\sqrt{7}}$$

Got it?

- Find the products of each radical expression:

$$(3 - 4\sqrt{2})(5 - 6\sqrt{2})$$

$$15 - 18\sqrt{2} - 20\sqrt{2} + 24(2) = \boxed{63 - 38\sqrt{2}}$$

$$(\sqrt{3} + \sqrt{5})^2 = (\sqrt{3} + \sqrt{5})(\sqrt{3} + \sqrt{5})$$

$$3 + \sqrt{15} + \sqrt{15} + 5$$

$$\boxed{8 + 2\sqrt{15}}$$

▪ Multiplying Conjugates

- Conjugates are expressions, like $\sqrt{a} + \sqrt{b}$ and $\sqrt{a} - \sqrt{b}$ that differ only in the signs of the second terms.

$$\bullet (5 - \sqrt{7})(5 + \sqrt{7})$$

$$25 + \cancel{5\sqrt{7}} - \cancel{5\sqrt{7}} - 7$$

$$\boxed{18}$$

Got it?

- What is each product?
 - $(3 + \sqrt{8})(3 - \sqrt{8})$

$$9 - 8 = \boxed{1}$$

- $(\sqrt{2} + \sqrt{5})(\sqrt{2} - \sqrt{5})$

$$2 - 5 = \boxed{-3}$$

▪ Rationalizing the Denominator

- How can you rewrite the expression with a rationalized denominator?

$$\bullet \frac{3\sqrt{2}}{\sqrt{5}-\sqrt{2}} \cdot \frac{(\sqrt{5}+\sqrt{2})}{(\sqrt{5}+\sqrt{2})}$$

$$\frac{3\sqrt{10} + 3\sqrt{4}}{5-2} = \frac{\cancel{3}\sqrt{10} + \cancel{3}(2)}{\cancel{3}}$$

$$\boxed{\sqrt{10} + 2}$$

Got it?

- Can you rewrite these expressions with rationalized denominators?

$$\bullet \frac{2\sqrt{7}}{\sqrt{3}-\sqrt{5}} \cdot \frac{(\sqrt{3}+\sqrt{5})}{(\sqrt{3}+\sqrt{5})}$$

$$\frac{2\sqrt{21} + 2\sqrt{35}}{3-5} = \frac{2\sqrt{21} + 2\sqrt{35}}{-2}$$

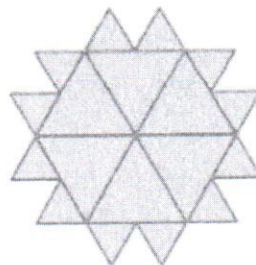
$$= \boxed{-\sqrt{21} - \sqrt{35}}$$

$$\bullet \frac{4x}{(3-\sqrt{6})} \cdot \frac{(3+\sqrt{6})}{(3+\sqrt{6})}$$

$$\frac{12x + 4x\sqrt{6}}{9-6} = \boxed{\frac{12x + 4x\sqrt{6}}{3}}$$

▪ STAMP QUESTION

- The design on a parquet floor, shown at the right, is made of equilateral triangles. The side of a large triangle is 6 in., and the side of a small triangle is 3 in. Find the total area of the design to the nearest tenth of a square inch.



Hint: Find the area of each individual triangle.