

Graph the following functions and find all of the critical information.

1. $y = \frac{x^2 - 36}{x + 4} = \frac{(x+6)(x-6)}{x+4}$

D: $(-\infty, -4) \cup (-4, \infty)$
 V: $x = -4$
 opp
 H: NONE
 X: $x = 6, x = -6$
 cross
 Y: $y = -9$
 E: $m = 2, n = 1$
 $m > n$
 SA@
 $y = x - 4$

$$\begin{array}{r} x-4 \overline{) x^2 + 0x - 36} \\ \underline{-(x^2 + 4x)} \\ 4x - 36 \\ \underline{-(-4x - 16)} \\ -20 \end{array}$$

2. $y = \frac{x^2 - x - 12}{x^2 + x - 2} = \frac{(x-4)(x+3)}{(x-1)(x+2)}$

D: $(-\infty, -2) \cup (-2, 1) \cup (1, \infty)$
 V: $x = -2, x = 1$
 opp
 H: NONE
 X: $x = 4, x = -3$
 cross
 Y: $y = 6$
 E: $m = 2, n = 2$
 $m = n$
 HA@ $y = 1$

3. Use the critical information to graph.

D: $(-\infty, -2) \cup (-2, 2) \cup (2, \infty)$
 V: $x = 2$, mult. 2, same
 $x = -2$ mult. 2 same
 H: NONE
 X: $(-5, 0)$ (5, 0)
 cross cross
 Y: $(0, -4)$
 E: $y = x^2$

4. Use the critical information to write the equation in factored form.

D: $(-\infty, -2) \cup (-2, -1) \cup (-1, 3) \cup (3, \infty)$
 V: $x = 3$, mult. 3, $x = -2$ mult. 2
 H: $(-1, 0)$
 X: $x = 0$ mult. 2, $x = -1$ mult. 1, $x = -5$ mult. 2
 Y: $(0, 0)$
 E: $y = \frac{3}{4}$

$$y = \frac{3x^2(x+1)^2(x+5)^2}{4(x+1)(x-3)^3(x+2)^2}$$

5. Simplify the rational expression.

$$\frac{v^2 + 10v + 21}{6v^2} \times \frac{1}{v+7}$$

$$\frac{\cancel{(v+7)}(v+3)}{6v^2} \cdot \frac{1}{\cancel{v+7}}$$

$$= \boxed{\frac{v+3}{6v^2}} \quad \boxed{v \neq 0, -7}$$

6. Solve the rational expression.

$$\frac{6}{n-6} = \frac{n+5}{n^2-6n} + \frac{1}{n^2-6n} \quad \text{ex. values}$$

$n \neq 6$
 $n \neq 0$

lcd: $n(n-6)$

$$n(n-6) \left(\frac{6}{n-6} \right) = n(n-6) \left(\frac{n+5}{n(n-6)} \right) + n(n-6) \left(\frac{1}{n(n-6)} \right)$$

$$6n = n+5+1$$

$$6n = n+6$$

$$\frac{-n}{-n} \quad \frac{-n}{-n}$$

$$\frac{5n}{5} = \frac{6}{5}$$

$$\frac{5n}{5} = \frac{6}{5}$$

$$\boxed{n = 6/5}$$

7. Use the graph to find all the critical information.

D: $(-\infty, -1) \cup$
 $(-1, 4) \cup (4, \infty)$

V: $x = -1, x = 4$
same opp

H: NONE

X: $x = -4, x = 3$
cross bounce

Y: $y = -10$

E: HA @ $y = 1$

